

EXTENDING COMPACT-TABLE TO BASIC SMART TABLES

CP2017

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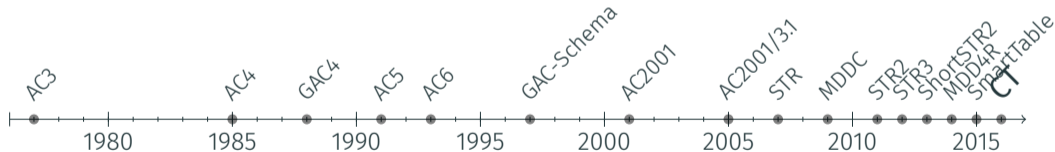
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Tables are the oldest most
used CP constraints

$$(x, y, z) \in$$

	x	y	z
τ_1	a	a	a
τ_2	d	d	a
τ_3	c	e	b
\vdots	\vdots	\vdots	\vdots



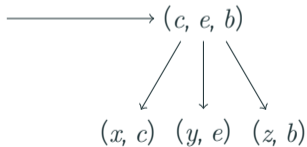
2016 : New algorithm ! CompactTable [CP2016], based on bitwise operations, completely outperformed existing algorithms.

COMPACT-TABLE [CP2016]

A Table

contains Tuples

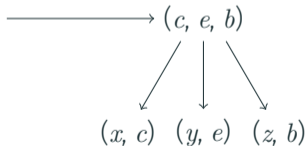
	x	y	z
τ_1	a	a	a
τ_2	c	e	b
τ_3	d	d	a
\vdots	\vdots	\vdots	\vdots



A Table

contains Tuples

	x	y	z
τ_1	a	a	a
τ_2	c	e	b
τ_3	d	d	a
\vdots	\vdots	\vdots	\vdots



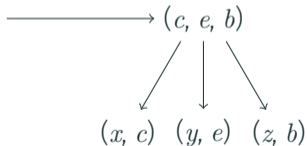
Set of the tuples of the Table

(x, a)	(x, d)
(x, b)	(x, e)
(x, c)	(x, f)

A Table

contains Tuples

	x	y	z
τ_1	a	a	a
τ_2	c	e	b
τ_3	d	d	a
\vdots	\vdots	\vdots	\vdots



Set of the tuples of the Table

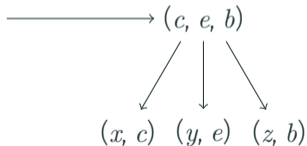
(x, a)	τ	(x, d)
(x, b)		(x, e)
(x, c)		(x, f)

For example: $\tau = (a, b, c)$

A Table

contains Tuples

	x	y	z
τ_1	a	a	a
τ_2	c	e	b
τ_3	d	d	a
\vdots	\vdots	\vdots	\vdots



Set of the tuples of the Table

(x, a)	(x, d)
(x, b)	τ (x, e)
(x, c)	(x, f)

For example: $\tau = (e, c, a)$

1. Which tuples are still valid?
2. Which values are no more supported?

1. Which tuples are still valid?

Update phase

2. Which values are no more supported?

1. Which tuples are still valid?

Update phase

2. Which values are no more supported?

Propagation phase

Goal of Update

Knowing which tuples are still valid

	Dom	Δ
x	{ a, b, c }	{ }
y	{ a, b, c }	{ }
z	{ a, b, c }	{ }

State

	x	y	z	
τ_1	a	a	a	✓
τ_2	a	b	c	✓
τ_3	c	a	b	✓
τ_4	b	c	c	✓
τ_5	a	c	a	✓

Table

τ_1	τ_2	τ_3	τ_4	τ_5
1	1	1	1	1

currTable

Goal of Update

Knowing which tuples are still valid

	Dom	Δ
x	{ a, x , c }	{ b }
y	{ a, b, c }	{ }
z	{ a, b, c }	{ }

State

	x	y	z	
τ_1	a	a	a	✓
τ_2	a	b	c	✓
τ_3	c	a	b	✓
τ_4	b	c	c	✗
τ_5	a	c	a	✓

Table

τ_1	τ_2	τ_3	τ_4	τ_5
1	1	1	0	1

currTable

Goal of Update

Knowing which tuples are still valid

	Dom	Δ
x	{ a, c }	{ b }
y	{ a, b, c }	{ }
z	{ a, b, c }	{ c }

State

	x	y	z	
τ_1	a	a	a	✓
τ_2	a	b	c	✗
τ_3	c	a	b	✓
τ_4	b	c	c	
τ_5	a	c	a	✓

Table

τ_1	τ_2	τ_3	τ_4	τ_5
1	0	1	0	1

currTable

Goal of Update

Knowing which tuples are still valid

	Dom	Δ
x	{ a, c }	{ a, b }
y	{ a, b, c }	{ }
z	{ a, b }	{ c }

State

	x	y	z	
τ_1	a	a	a	X
τ_2	a	b	c	
τ_3	c	a	b	✓
τ_4	b	c	c	
τ_5	a	c	a	X

Table

τ_1	τ_2	τ_3	τ_4	τ_5
0	0	1	0	0

currTable

	x	y	z
τ_1	a	a	a
τ_2	a	b	c
τ_3	c	a	b
τ_4	b	c	c
τ_5	a	c	a

Table

	τ_1	τ_2	τ_3	τ_4	τ_5
(x,a)					
(x,b)					
(x,c)					
(y,a)					
(y,b)					
(y,c)					
(z,a)					
(z,b)					
(z,c)					

support

	x	y	z
τ_1	a	a	a
τ_2	a	b	c
τ_3	c	a	b
τ_4	b	c	c
τ_5	a	c	a

Table

	τ_1	τ_2	τ_3	τ_4	τ_5
(x,a)	1				
(x,b)	0				
(x,c)	0				
(y,a)	1				
(y,b)	0				
(y,c)	0				
(z,a)	1				
(z,b)	0				
(z,c)	0				

support

	x	y	z
τ_1	a	a	a
τ_2	a	b	c
τ_3	c	a	b
τ_4	b	c	c
τ_5	a	c	a

Table

	τ_1	τ_2	τ_3	τ_4	τ_5
(x,a)	1	1			
(x,b)	0	0			
(x,c)	0	0			
(y,a)	1	0			
(y,b)	0	1			
(y,c)	0	0			
(z,a)	1	0			
(z,b)	0	0			
(z,c)	0	1			

support

	x	y	z
τ_1	a	a	a
τ_2	a	b	c
τ_3	c	a	b
τ_4	b	c	c
τ_5	a	c	a

Table

	τ_1	τ_2	τ_3	τ_4	τ_5
(x,a)	1	1	0		
(x,b)	0	0	0		
(x,c)	0	0	1		
(y,a)	1	0	1		
(y,b)	0	1	0		
(y,c)	0	0	0		
(z,a)	1	0	0		
(z,b)	0	0	1		
(z,c)	0	1	0		

support

	x	y	z
τ_1	a	a	a
τ_2	a	b	c
τ_3	c	a	b
τ_4	b	c	c
τ_5	a	c	a

Table

	τ_1	τ_2	τ_3	τ_4	τ_5
(x,a)	1	1	0	0	
(x,b)	0	0	0	1	
(x,c)	0	0	1	0	
(y,a)	1	0	1	0	
(y,b)	0	1	0	0	
(y,c)	0	0	0	1	
(z,a)	1	0	0	0	
(z,b)	0	0	1	0	
(z,c)	0	1	0	1	

support

	x	y	z
τ_1	a	a	a
τ_2	a	b	c
τ_3	c	a	b
τ_4	b	c	c
τ_5	a	c	a

Table

	τ_1	τ_2	τ_3	τ_4	τ_5
(x,a)	1	1	0	0	1
(x,b)	0	0	0	1	0
(x,c)	0	0	1	0	0
(y,a)	1	0	1	0	0
(y,b)	0	1	0	0	0
(y,c)	0	0	0	1	1
(z,a)	1	0	0	0	1
(z,b)	0	0	1	0	0
(z,c)	0	1	0	1	0

support

	x	y	z
τ_1	a	a	a
τ_2	a	b	c
τ_3	c	a	b
τ_4	b	c	c
τ_5	a	c	a

Table

	τ_1	τ_2	τ_3	τ_4	τ_5
(x,a)	1	1	0	0	1
(x,b)	0	0	0	1	0
(x,c)	0	0	1	0	0
(y,a)	1	0	1	0	0
(y,b)	0	1	0	0	0
(y,c)	0	0	0	1	1
(z,a)	1	0	0	0	1
(z,b)	0	0	1	0	0
(z,c)	0	1	0	1	0

support

Set of Tuples

(x,a)
(x,b)
(x,c)

Sets

	x	y	z
τ_1	a	a	a
τ_2	a	b	c
τ_3	c	a	b
τ_4	b	c	c
τ_5	a	c	a

Table

	τ_1	τ_2	τ_3	τ_4	τ_5
(x,a)	1	1	0	0	1
(x,b)	0	0	0	1	0
(x,c)	0	0	1	0	0
(y,a)	1	0	1	0	0
(y,b)	0	1	0	0	0
(y,c)	0	0	0	1	1
(z,a)	1	0	0	0	1
(z,b)	0	0	1	0	0
(z,c)	0	1	0	1	0

support

Set of Tuples

(x,a)	τ_1	τ_2	τ_5
(x,b)			
(x,c)			

Sets

	x	y	z
τ_1	a	a	a
τ_2	a	b	c
τ_3	c	a	b
τ_4	b	c	c
τ_5	a	c	a

Table

	τ_1	τ_2	τ_3	τ_4	τ_5
(x,a)	1	1	0	0	1
(x,b)	0	0	0	1	0
(x,c)	0	0	1	0	0
(y,a)	1	0	1	0	0
(y,b)	0	1	0	0	0
(y,c)	0	0	0	1	1
(z,a)	1	0	0	0	1
(z,b)	0	0	1	0	0
(z,c)	0	1	0	1	0

support

Set of Tuples

(x,a)
(x,b)
(x,c) τ_3

Sets

Set of Tuples in Table

(x,a)	(x,d)
(x,b)	(x,e)
(x,c)	(x,f)

Goal of the update

Remove invalid tuples from `currTable`

Set of Tuples in Table

(x,a)		(x,d)
(x,b)	Valid tuples	(x,e)
(x,c)		(x,f)

Goal of the update

Remove invalid tuples from `currTable`

Set of Tuples in Table

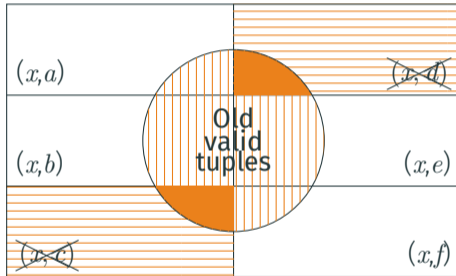
(x,a)	(x,d)
(x,b)	(x,e)
(x,c)	(x,f)

Old valid tuples

Goal of the update

Remove invalid tuples from `currTable`

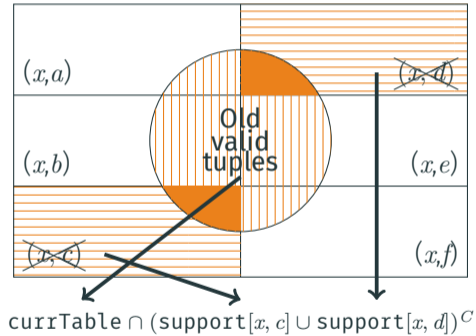
Set of Tuples in Table



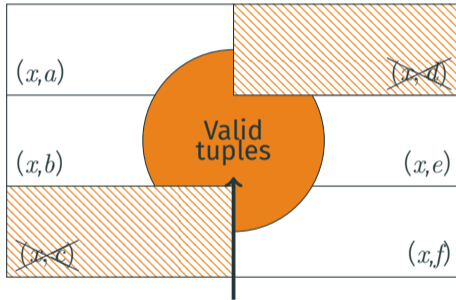
Goal of the update

Remove invalid tuples from `currTable`

Set of Tuples in Table

**Goal of the update**Remove invalid tuples from `currTable`

Set of Tuples in Table

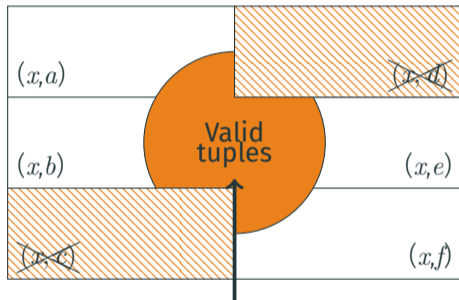


$$\text{currTable} \cap (\text{support}[x, c] \cup \text{support}[x, d])^C$$

Goal of the update

Remove invalid tuples from `currTable`

Set of Tuples in Table



$$\text{currTable} \cap (\text{support}[x, c] \cup \text{support}[x, d])^C$$

Goal of the update

Remove invalid tuples from `currTable`

Algorithm: ClassicalUpdate(x)

- 1 $\text{mask} \leftarrow 0$;
 - 2 **foreach** value $a \in \Delta_x$ **do**
 - 3 $\text{mask} \leftarrow \text{mask} \mid \text{supports}[x, a]$;
 - 4 $\text{mask} \leftarrow \sim \text{mask}$;
 - 5 $\text{currTable} \leftarrow \text{currTable} \& \text{mask}$;
-

Set of Tuples in Table

(x,a)		(x,d)
(x,b)	Valid tuples	(x,e)
(x,c)		(x,f)

Goal of the update

Remove invalid tuples from `currTable`

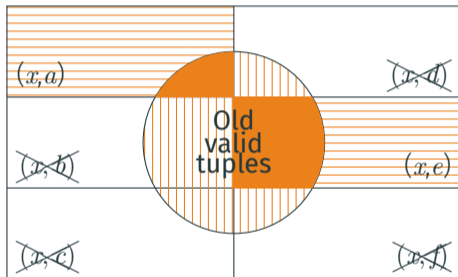
Set of Tuples in Table

(x, a)		(x, d)
(x, b)	Old valid tuples	(x, e)
(x, c)		(x, f)

Goal of the update

Remove invalid tuples from `currTable`

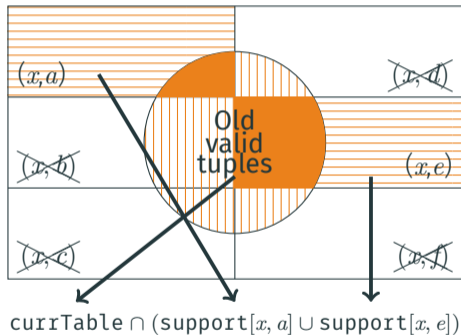
Set of Tuples in Table



Goal of the update

Remove invalid tuples from `currTable`

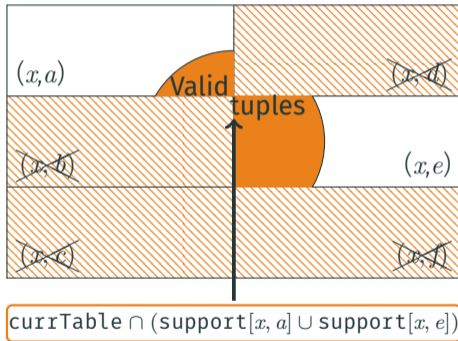
Set of Tuples in Table



Goal of the update

Remove invalid tuples from `currTable`

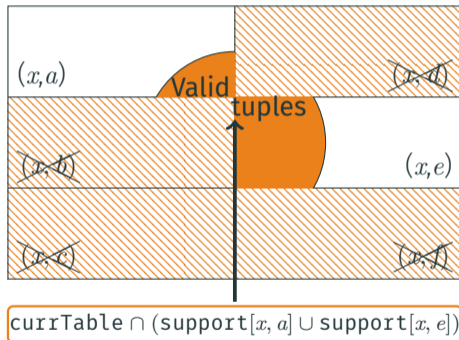
Set of Tuples in Table



Goal of the update

Remove invalid tuples from `currTable`

Set of Tuples in Table



Goal of the update

Remove invalid tuples from `currTable`

Algorithm: ResetUpdate(x)

- 1 `mask` \leftarrow 0 ;
 - 2 **foreach** value $a \in \text{dom}(x)$ **do**
 - 3 `mask` \leftarrow `mask` | `supports`[x, a] ;
 - 4 `currTable` \leftarrow `currTable` & `mask` ;
-

- Classical update :

$$\mathcal{O}(|\Delta_x|)$$

- Reset update :

$$\mathcal{O}(|dom(x)|)$$

Goal of the update

Remove invalid tuples from `currTable`

Algorithm: Update(x)

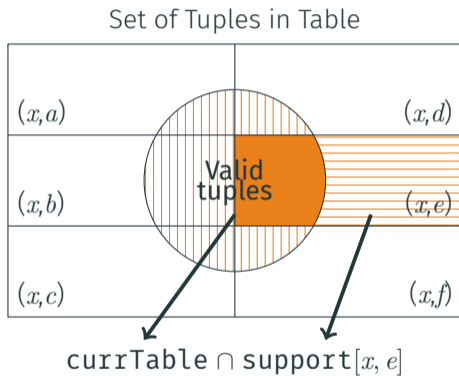
```
1 foreach variable  $x \in scp$  where  $|\Delta_x| > 0$  do
2   if  $|\Delta_x| < |dom(x)|$  then
3     ClassicalUpdate(x);
4   else
5     ResetUpdate(x);
```

Set of Tuples in Table

(x, a)		(x, d)
(x, b)	Valid tuples	(x, e)
(x, c)		(x, f)

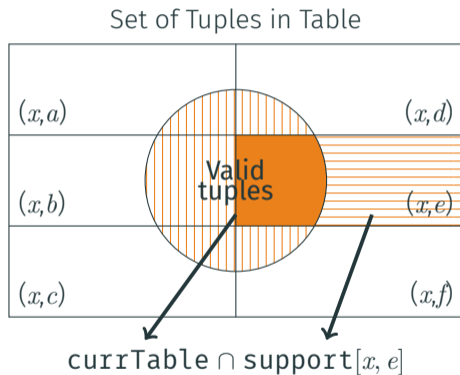
Goal of the propagation

Remove unsupported values



Goal of the propagation

Remove unsupported values



Goal of the propagation

Remove unsupported values

Algorithm: Propagate()

```

1 foreach variable  $x \in \text{scp}$  do
2   foreach value  $a \in \text{dom}(x)$  do
3     if  $\text{currTable} \ \& \ \text{supports}[x, a] = 0$ 
4       then
           $\text{dom}(x) \leftarrow \text{dom}(x) \setminus \{a\}$ ;

```


COMPACT-TABLE FOR BASIC SMART TUPLES

A Basic Smart Table

	x	y	z
τ_1	*	*	$\in \{a, b\}$
τ_2	$\neq a$	c	$\leq a$
τ_3	b	*	*
τ_4	$\geq c$	$\neq b$	a
	\vdots	\vdots	\vdots

A Basic Smart Table

contains Smart Elements

representing multiples values

	x	y	z
τ_1	*	*	$\in \{a, b\}$
τ_2	$\neq a$	c	$\leq a$
τ_3	b	*	*
τ_4	$\geq c$	$\neq b$	a
	\vdots	\vdots	\vdots

A Basic Smart Table

contains Smart Elements

representing multiples values

	x	y	z
τ_1	*	*	$\in \{a, b\}$
τ_2	$\neq a$	c	$\leq a$
τ_3	b	*	*
τ_4	$\geq c$	$\neq b$	a
	\vdots	\vdots	\vdots

single value: e

~~x~~ , ~~x~~ , ~~x~~ , ~~x~~ , **e** , ~~x~~

A Basic Smart Table

contains Smart Elements

representing multiples values

	x	y	z
τ_1	*	*	$\in \{a, b\}$
τ_2	$\neq a$	c	$\leq a$
τ_3	b	*	*
τ_4	$\geq c$	$\neq b$	a
	\vdots	\vdots	\vdots

single value: e

universal value: *

~~a~~ , ~~b~~ , ~~c~~ , ~~d~~ , e , ~~f~~

a , b , c , d , e , f

A Basic Smart Table

contains Smart Elements

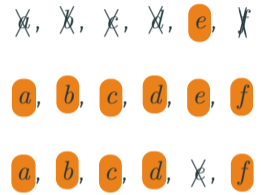
representing multiples values

	x	y	z
τ_1	*	*	$\in \{a, b\}$
τ_2	$\neq a$	c	$\leq a$
τ_3	b	*	*
τ_4	$\geq c$	$\neq b$	a
	\vdots	\vdots	\vdots

single value: e

universal value: *

exclusion: $\neq e$



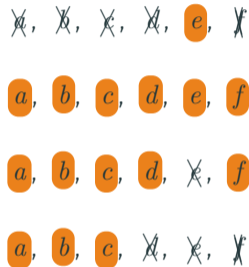
A Basic Smart Table

contains Smart Elements

representing multiples values

	x	y	z
τ_1	*	*	$\in \{a, b\}$
τ_2	$\neq a$	c	$\leq a$
τ_3	b	*	*
τ_4	$\geq c$	$\neq b$	a
	\vdots	\vdots	\vdots

- single value: e
- universal value: $*$
- exclusion: $\neq e$
- upper bound: $\leq c$

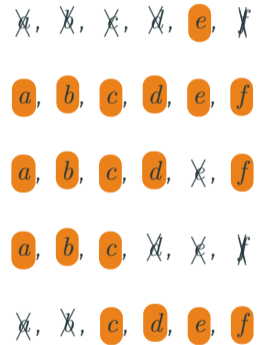
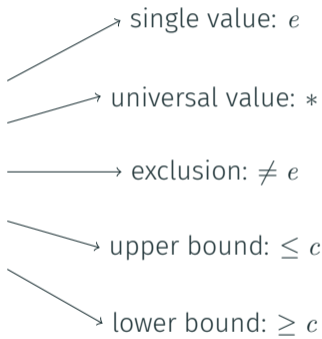


A Basic Smart Table

	x	y	z
τ_1	*	*	$\in \{a, b\}$
τ_2	$\neq a$	c	$\leq a$
τ_3	b	*	*
τ_4	$\geq c$	$\neq b$	a
	\vdots	\vdots	\vdots

contains Smart Elements

representing multiples values

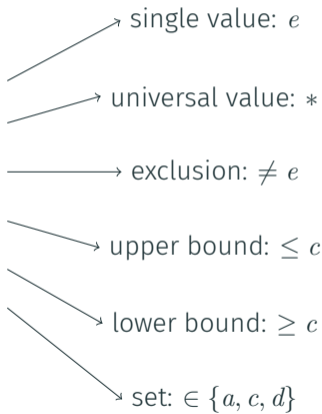


A Basic Smart Table

contains Smart Elements

representing multiples values

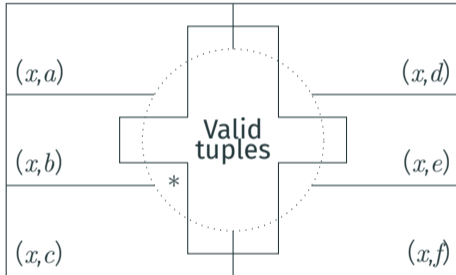
	x	y	z
τ_1	*	*	$\in \{a, b\}$
τ_2	$\neq a$	c	$\leq a$
τ_3	b	*	*
τ_4	$\geq c$	$\neq b$	a
	\vdots	\vdots	\vdots



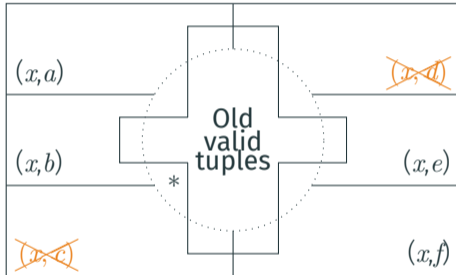
Set of Tuples in Table

(x,a)		(x,d)
(x,b)	*	(x,e)
(x,c)		(x,f)

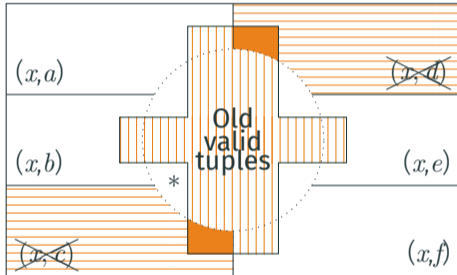
Set of Tuples in Table



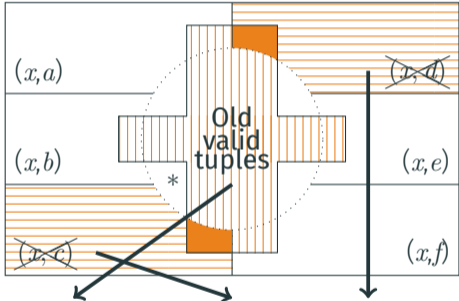
Set of Tuples in Table



Set of Tuples in Table

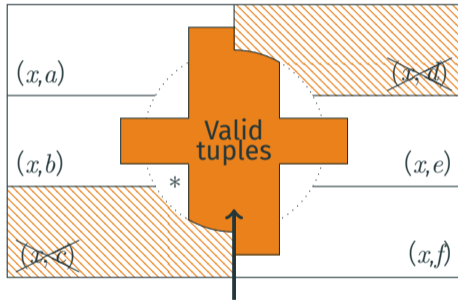


Set of Tuples in Table



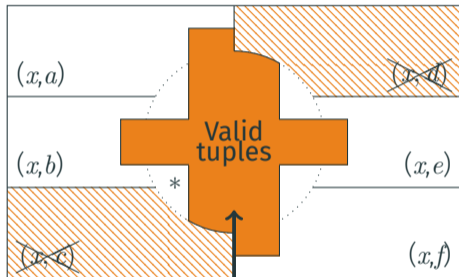
$$\text{currTable} \cap (\text{support}^*[x, c] \cup \text{support}^*[x, d])^C$$

Set of Tuples in Table



$$\text{currTable} \cap (\text{support}^*[x, c] \cup \text{support}^*[x, d])^C$$

Set of Tuples in Table



$$\text{currTable} \cap (\text{support}^*[x, c] \cup \text{support}^*[x, d])^C$$

Algorithm: ClassicalUpdate(x)

- 1 mask \leftarrow 0;
 - 2 **foreach** value $a \in \Delta_x$ **do**
 - 3 | mask \leftarrow mask | support^{*}[x, a];
 - 4 mask \leftarrow \sim mask;
 - 5 currTable \leftarrow currTable & mask;
-

$$|dom(x)| == 0$$

$$|dom(x)| > 1$$

$$|dom(x)| == 1$$

$$|dom(x)| == 0$$

Trivial!
Handled by variable x

$$|dom(x)| > 1$$

$$|dom(x)| == 1$$

$$|dom(x)| == 0$$

Trivial!
Handled by variable x

$$|dom(x)| > 1$$

$$|dom(x)| == 1$$

$|\Delta_x| \geq |dom(x)|$ always true!
ResetUpdate(x) used
and already working!

$$|dom(x)| == 0$$

Trivial!
Handled by variable x

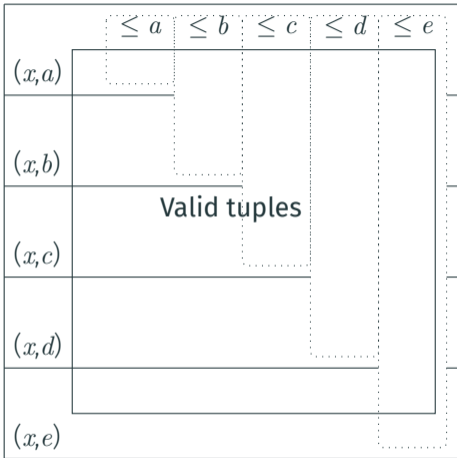
$$|dom(x)| == 1$$

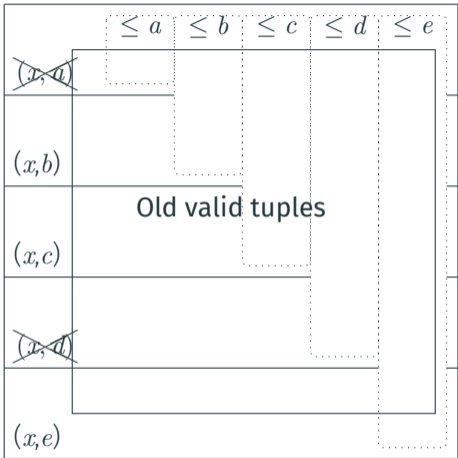
$|\Delta_x| \geq |dom(x)|$ always true!
ResetUpdate(x) used
and already working!

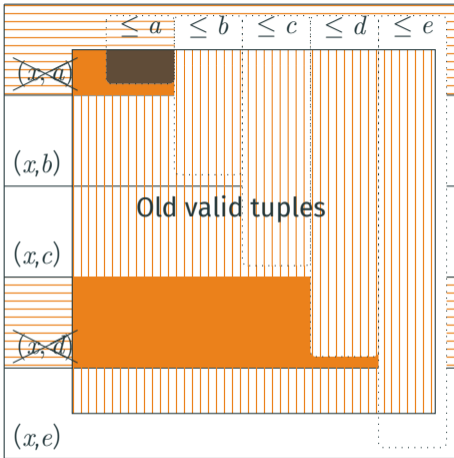
$$|dom(x)| > 1$$

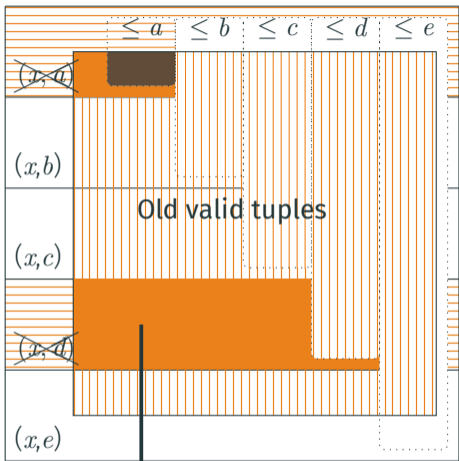
If $|\Delta_x| < |dom(x)|$
Tuple always valid!
At least one valid value
support*[x][τ] = 0

If $|\Delta_x| \geq |dom(x)|$
ResetUpdate(x) used
and already working!

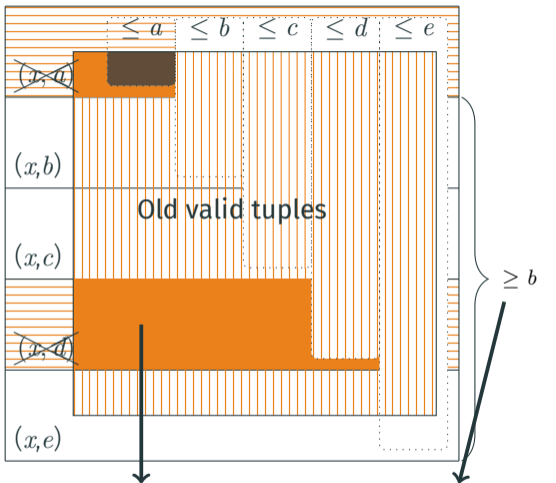




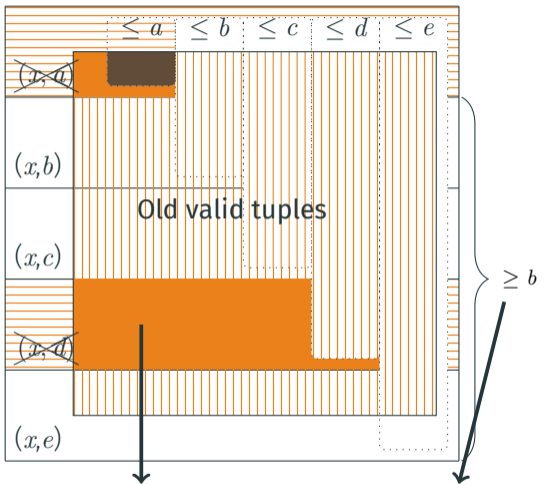




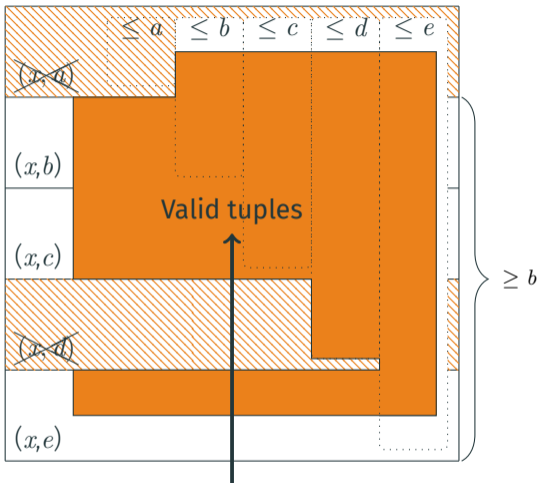
$$\text{currTable} \cap \left(\text{support}^*[x, a] \cup \text{support}^*[x, d] \right) C$$



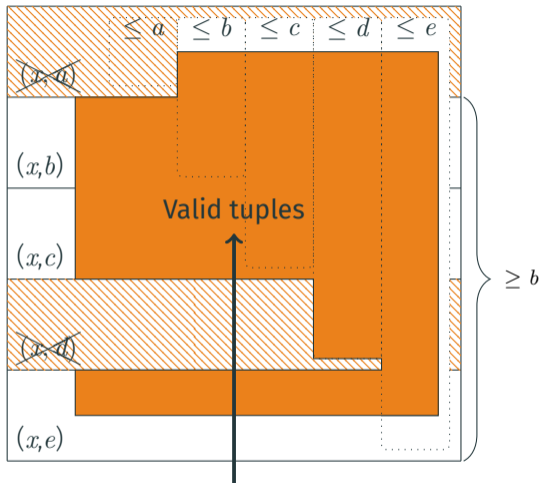
$$\text{currTable} \cap \left(\text{support}^*[x, a] \cup \text{support}^*[x, d] \right) \cap \text{supportMin}[x, b]$$



$$\text{currTable} \cap \left(\frac{\text{support}^*[x, a]}{\cup} \text{support}^*[x, d] \right) \cap \text{supportMin}[x, b]$$



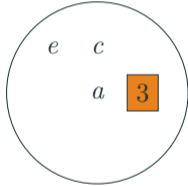
$$\text{currTable} \cap \left(\frac{\text{support}^*[x, a]}{\cup} \right) C \cap \text{supportMin}[x, b]$$

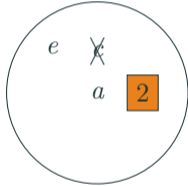


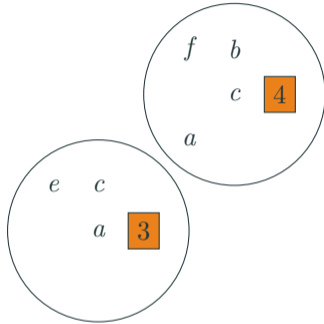
$$\text{currTable} \cap \left(\bigcup_{\substack{\text{support}^*[x, a] \\ \text{support}^*[x, d]}} \right) C \cap \text{supportMin}[x, b]$$

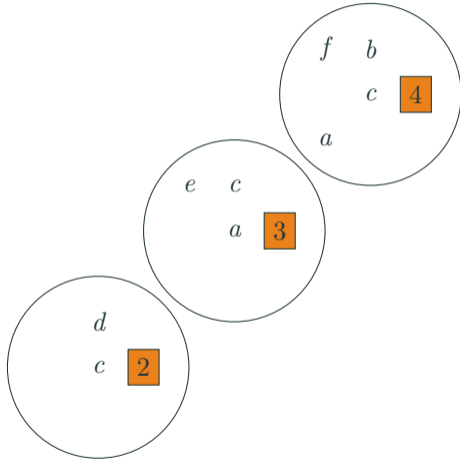
Algorithm: ClassicalUpdate(x)

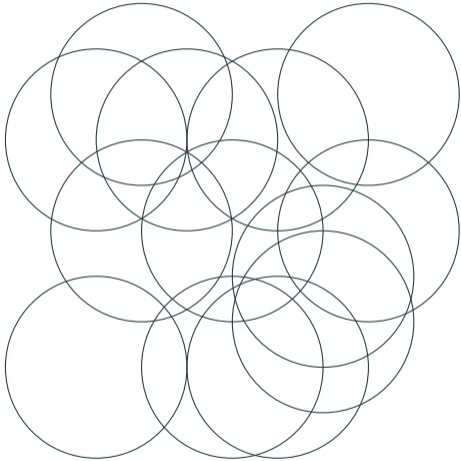
- 1 $\text{mask} \leftarrow 0$;
- 2 **foreach** value $a \in \Delta_x$ **do**
- 3 **if** $a \in [\text{dom}(x).\text{min}; \text{dom}(x).\text{max}]$
- 4 **then**
- 5 $\text{mask} \leftarrow \text{mask} \mid$
- 6 $\text{support}^*[x, a]$;
- 7 $\text{mask} \leftarrow \sim \text{mask}$;
- 8 $\text{mask} \leftarrow \text{mask} \&$
- 9 $\text{supportMin}[x, \text{dom}(x).\text{min}]$;
- 10 $\text{mask} \leftarrow \text{mask} \&$
- 11 $\text{supportMax}[x, \text{dom}(x).\text{max}]$;
- 12 $\text{currTable} \leftarrow \text{currTable} \& \text{mask}$;

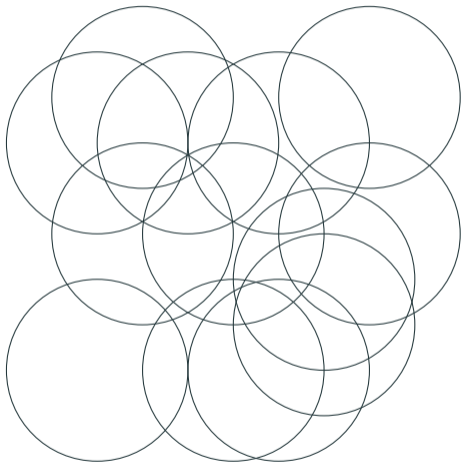












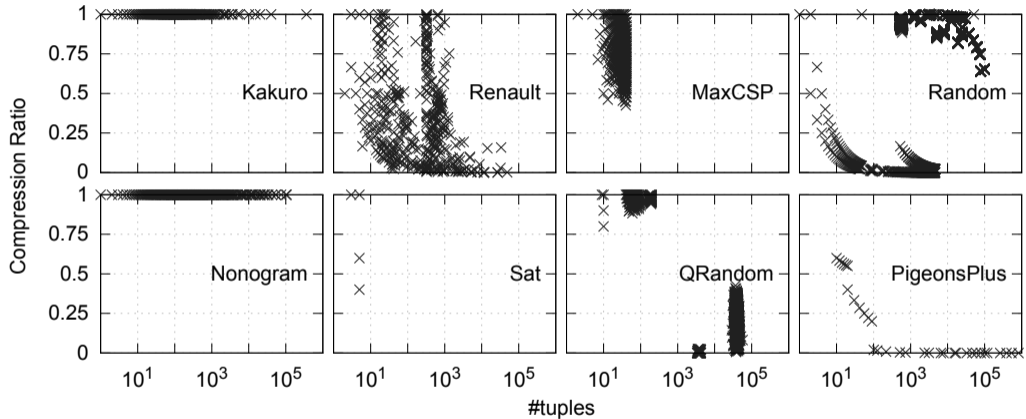
Algorithm: ResetUpdate(x)

- 1 `mask` \leftarrow 0 ;
 - 2 **foreach** value $a \in \text{dom}(x)$ **do**
 - 3 `mask` \leftarrow `mask` | `supports[x, a]` ;
 - 4 `currTable` \leftarrow `currTable` & `mask` ;
-

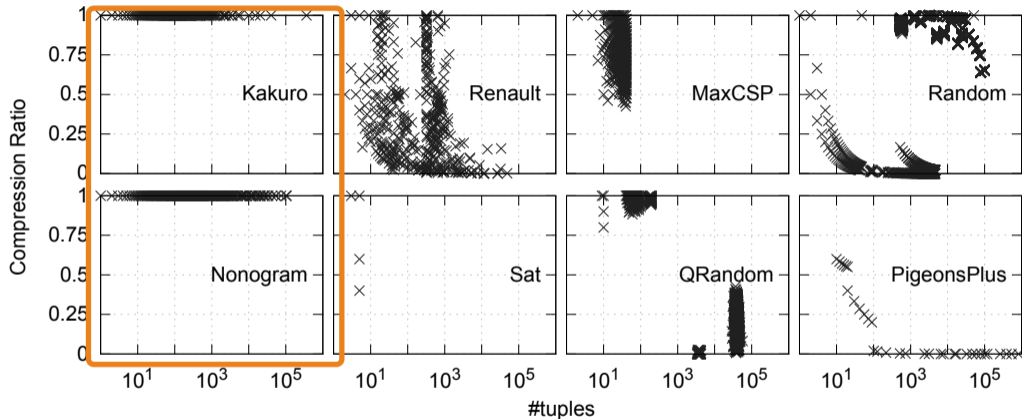
Algorithm: Update(x)

```
1 foreach variable  $x \in \text{scp}_{no \in S}$  do
2   if  $|\Delta_x| < |dom(x)|$  then
3     | ClassicalUpdate(x);
4   else
5     | ResetUpdate(x);
6 foreach variable  $x \in \text{scp}_{with \in S}$  do
7   | ResetUpdate(x);
```

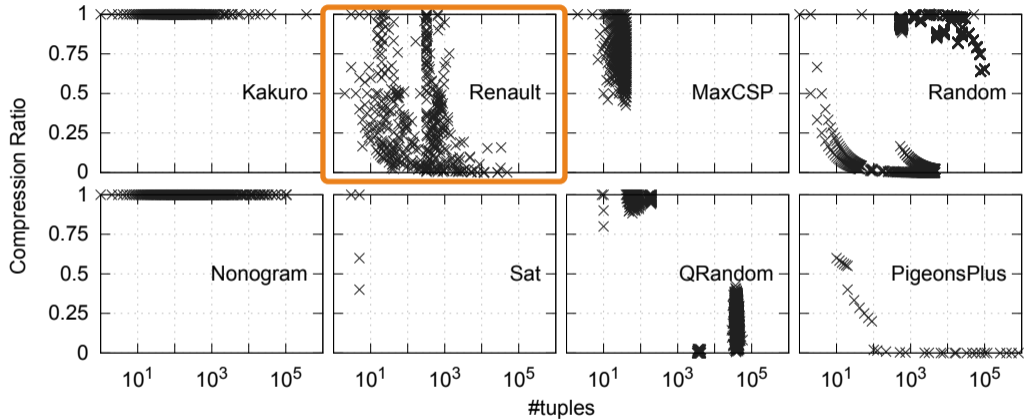
RESULTS



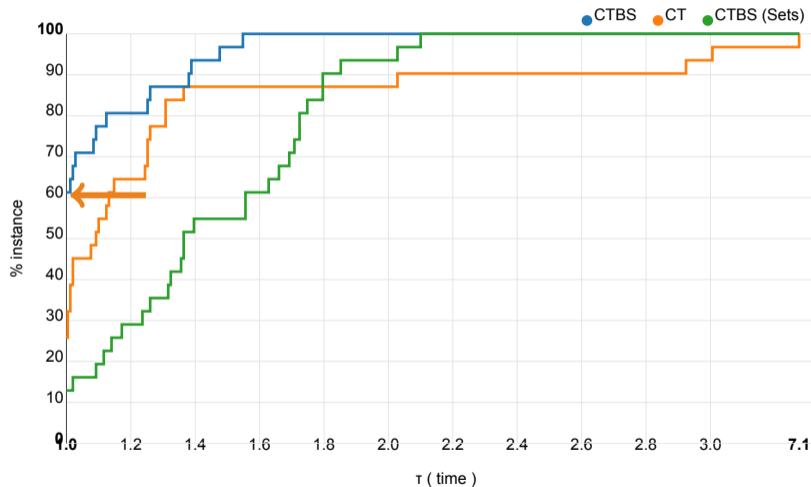
Greedy compression algorithm generating \leq and \geq



Greedy compression algorithm generating \leq and \geq

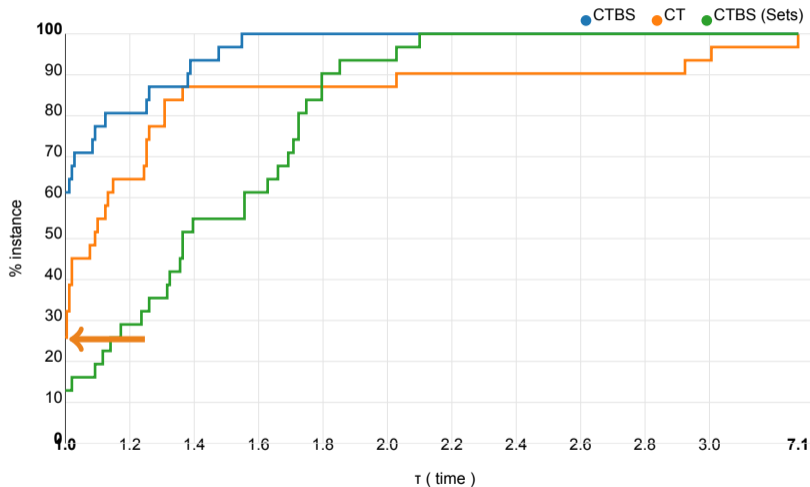


Greedy compression algorithm generating \leq and \geq



CTBS: compression
 \leq & \geq + post
 processing
 \neq & *

CTBS (Sets): same
 compressions
 but seen as $\in \mathcal{S}$



CTBS: compression
 \leq & \geq + post
 processing
 \neq & *

CTBS (Sets): same
 compressions
 but seen as $\in \mathcal{S}$

$ dom(x) $	sets		structured sets	
1	$\{a\}$	1	*	1
2	$\{a\}, \{b\}, \{a, b\}$	3	$a, b, *$	3
3	$\{a\}, \{b\}, \{c\}, \{a, b\},$ $\{a, c\}, \{b, c\}, \{a, b, c\}$	7	$a, b, c, \neq a,$ $\neq b, \neq c, *$	7
4	$\{a\}, \{b\}, \dots, \{a, b\}, \{a, c\},$ $\{a, d\}, \{b, c\}, \{b, d\}, \{c, d\},$ $\{a, b, c\}, \dots, \{a, b, c, d\}$	15	$a, b, c, d,$ $\leq b, \geq c, \neq a,$ $\neq b, \neq c, \neq d, *$	11
5	$\{a\}, \{b\}, \dots, \{a, b\}, \{a, c\}, \{a, d\}, \{a, e\},$ $\{b, c\}, \{b, d\}, \{b, e\}, \{c, d\}, \{c, e\},$ $\{a, b, c\}, \{a, b, d\}, \{a, b, e\}, \{a, c, d\},$ $\{a, c, e\}, \dots, \{a, b, c, d\}, \dots, \{a, b, c, d, e\}$	31	a, b, c, d, e $\leq b, \leq c, \geq c,$ $\geq d, \neq a, \neq b,$ $\neq c, \neq d, \neq e, *$	15

CONCLUSION

Tuples

CT
[CP2016]

	x	y	z
τ_1	a	a	b
τ_2	b	c	a
τ_3	b	a	a
τ_4	c	b	c

Short tuples

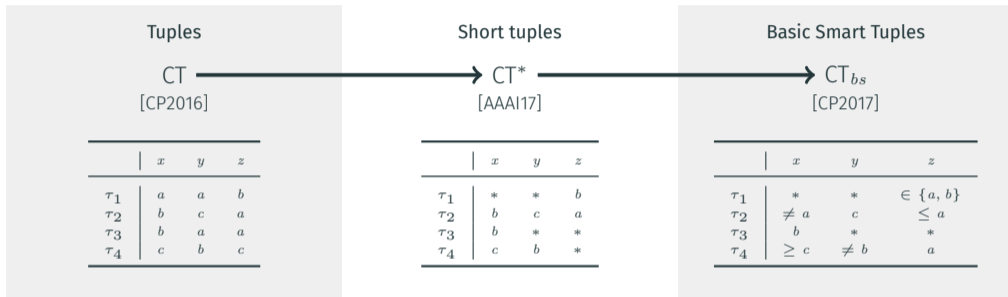
CT*
[AAAI17]

	x	y	z
τ_1	*	*	b
τ_2	b	c	a
τ_3	b	*	*
τ_4	c	b	*

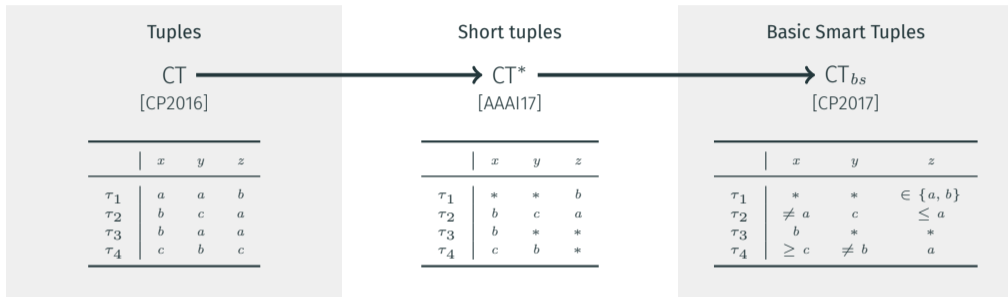
Basic Smart Tuples

CT_{bs}
[CP2017]

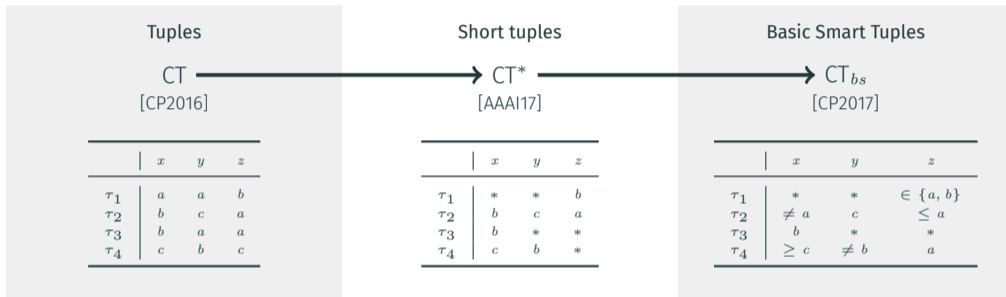
	x	y	z
τ_1	*	*	$\in \{a, b\}$
τ_2	$\neq a$	c	$\leq a$
τ_3	b	*	*
τ_4	$\geq c$	$\neq b$	a



- Increase expressiveness

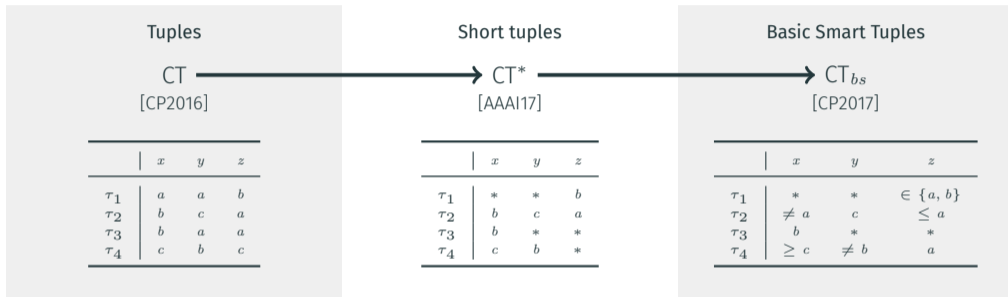


- Increase expressiveness
- Decrease storage memory



- Increase expressiveness
- Decrease storage memory

- Increase speed



- Increase expressiveness
- Decrease storage memory

- Increase speed
- Increase efficiency

Thank you for listening!

Any questions?