

# THE EXTENSIONAL CONSTRAINT

Doctoral Program CP2019

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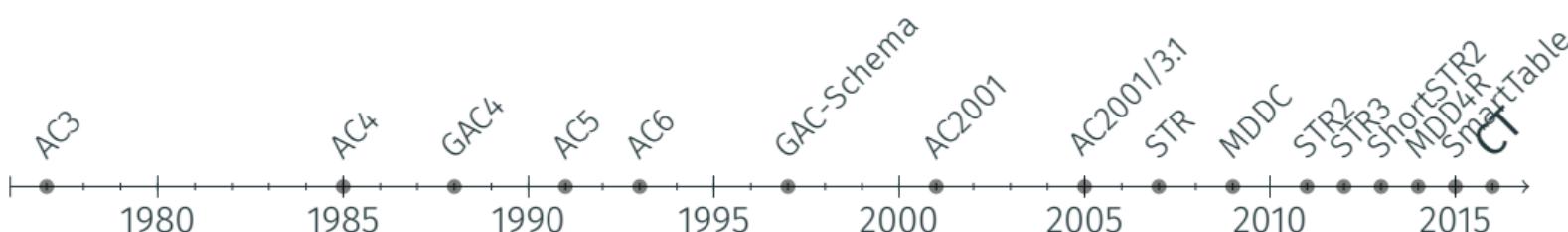
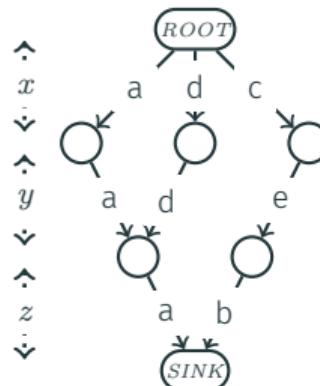
Advisor: Pierre Schaus



	$x$	$y$	$z$
$\tau_1$	$a$	$a$	$a$
$\tau_2$	$d$	$d$	$a$
$\tau_3$	$c$	$e$	$b$
$\vdots$	$\vdots$	$\vdots$	$\vdots$

Tables are the oldest most used CP constraints

MDDs are equivalent to tables



2016 : New algorithm! Compact-Table [CP2016], based on bitwise operations, completely outperformed existing algorithms

CT

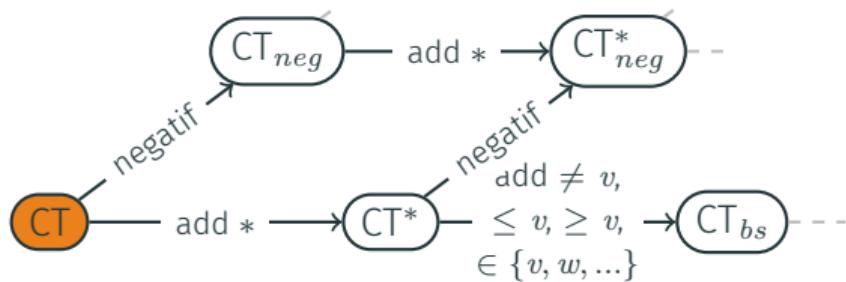
	$x_1$	$x_2$	$x_3$
$\tau_1$	$a$	$c$	$a$
$\tau_2$	$b$	$b$	$b$
$\tau_3$	$a$	$c$	$b$
$\tau_4$	$c$	$a$	$b$
$\tau_5$	$b$	$c$	$b$
$\tau_6$	$c$	$b$	$c$
$\tau_7$	$a$	$a$	$b$
$\tau_8$	$b$	$b$	$c$

Input of CT: A positive Table (contains accepted solutions)



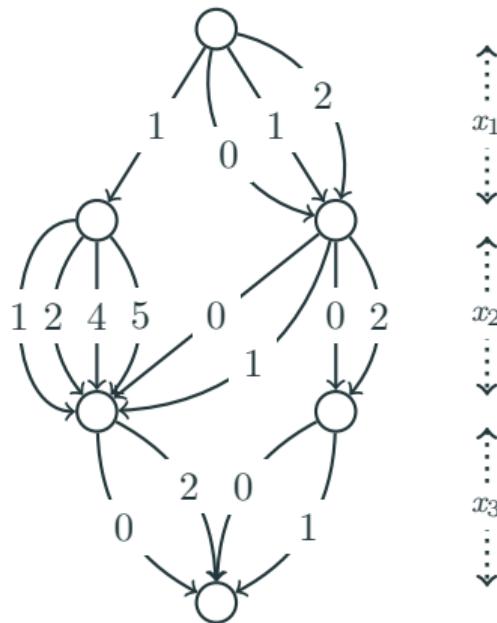
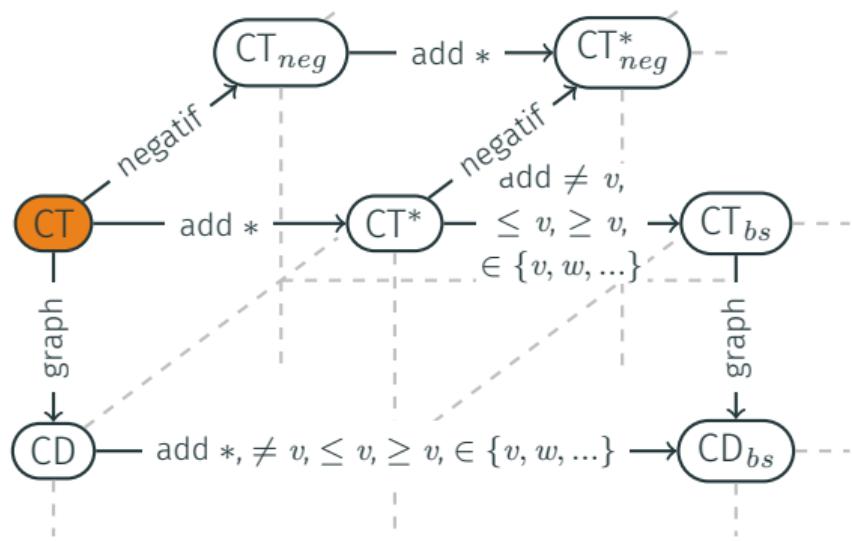
	$x$	$y$	$z$
$\tau_1$	*	*	$\in \{a, b\}$
$\tau_2$	$\neq a$	$c$	$\leq a$
$\tau_3$	$b$	*	*
$\tau_4$	$\geq c$	$\neq b$	$a$
	:	:	:

Input of CT<sub>bs</sub>: A positive Basic Smart Table (unary compression using \*, ≠, ≤, ≥, ∈)

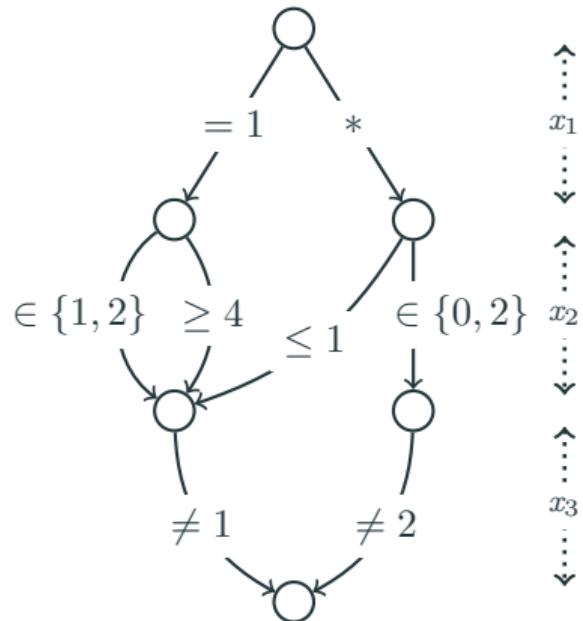
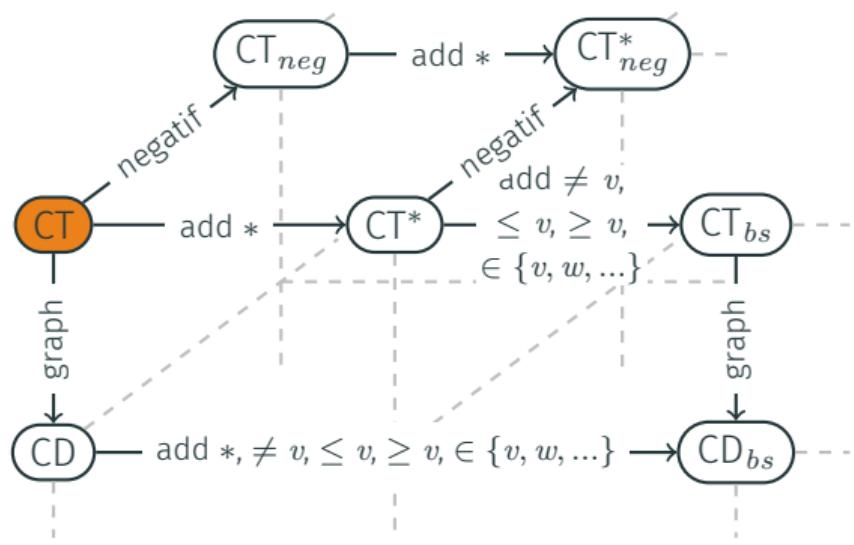


	$x_1$	$x_2$	$x_3$
$\tau_1$	$a$	$c$	$a$
$\tau_2$	$b$	$b$	$b$
$\tau_3$	$a$	$c$	$b$
$\tau_4$	$c$	$a$	$b$
$\tau_5$	$b$	$c$	$b$
$\tau_6$	$c$	$b$	$c$
$\tau_7$	$a$	$a$	$b$
$\tau_8$	$b$	$b$	$c$

Input of **CT<sub>neg</sub>**: A negative Table (contains rejected solutions)



Input of **CD**: A positive MDD or MVD (layered diagram)



Input of **CD<sub>bs</sub>**: A positive Basic smart MDD or MVD

- Modelling:
  - increase expressiveness
  - various tools available for users:  
Tables, Negative Tables, Basic Smart Tables, MDDs/MVDs, Basic Smart MDDs/MVDs
  - reduction of the storage size
- Propagators:
  - efficient algorithms
  - increased resolution speed
  - no model decompression

- H. Verhaeghe, C. Lecoutre and P. Schaus. **Extending Compact-Table to Negative and Short Tables.** AAAI17
- H. Verhaeghe, C. Lecoutre, Y. Deville and P. Schaus. **Extending Compact-Table to Basic Smart Tables.** CP2017
- H. Verhaeghe, C. Lecoutre, P. Schaus. **Compact-MDD: Efficiently filtering (s)mdd constraints with Reversible Sparse Bit-Sets.** IJCAI18
- H. Verhaeghe, C. Lecoutre, P. Schaus. **Extending Compact-Diagram to Basic Smart Multi-Valued Variable Diagrams.** CPAIOR19